

Lab 14 Answers

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$$n = 793$$

	Reinforced Burrow	Non-Reinforced Burrow	Total
a) Injured	17	218	235
Not Injured	130	428	558
Total	147	646	793



$$b) OR = \frac{17(428)}{218(130)} \approx 0.257$$

The odds of a groundhog experiencing an injury given they had a reinforced burrow is 0.257 times the odds of a groundhog experiencing an injury given they did not have a reinforced burrow. This OR makes it seem as if there is a benefit to using a reinforced burrow since it is less than 1. BUT! a CI should be constructed to understand the possible range of the benefit.

$$c) \text{Formula: } \log(OR) \pm 1.96 \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}} \quad \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}} = \sqrt{\frac{1}{17} + \frac{1}{218} + \frac{1}{130} + \frac{1}{428}} = 0.270997$$

$$\text{CI for } \log(OR) = \log(0.257) \pm 1.96(0.270997) \\ = (-1.8898, -0.8275)$$

$$\text{CI for } OR = (\exp\{-1.8898\}, \exp\{-0.8275\}) \\ = (0.151, 0.437)$$

Since this CI is entirely below 1, there is evidence that reinforced burrows help prevent injuries.

$$d) E_1 = \frac{235(147)}{793} \quad E_2 = \frac{235(646)}{793} \quad E_3 = \frac{558(147)}{793} \quad E_4 = \frac{558(646)}{793} \\ = 43.5624 \quad = 191.4376 \quad = 103.4376 \quad = 454.5624$$

e) H_0 : There is an association between burrow type and injury vs

H_a : There is no association between burrow type and injury

$$\chi^2 = \sum_{i=1}^4 \frac{(O_i - E_i)^2}{E_i} = \frac{(17 - 43.5624)^2}{43.5624} + \frac{(218 - 191.4376)^2}{191.4376} + \frac{(130 - 103.4376)^2}{103.4376} + \frac{(428 - 454.5624)^2}{454.5624} \\ \approx 27.6 \text{ with } df = 1$$

Approximate p-value: $27.6 \Rightarrow$ area to the left $\gg 0.959$

We want area to the right so our p-value $\ll 1 - 0.959 \Rightarrow$ our p-value $\ll 0.041$

Conclusion: The χ^2 test provides evidence of an association between burrow type and injuries for groundhogs.

② a) If the data are normally distributed a t-test would be the most appropriate.

The standard deviations and sample sizes should be considered when determining the type of t-test to perform.

b) Let M_W = average fire efficiency for Western dragons and

M_E = average fire efficiency for Eastern dragons

Hypotheses: $H_0: M_W = M_E$ vs $H_a: M_W \neq M_E$

$$\text{Test Statistic: } t = \frac{\bar{X}_W - \bar{X}_E}{SE} \quad \text{where } SE = 6.343 \sqrt{\frac{1}{249} + \frac{1}{79}} = 0.8191$$
$$= \frac{20.145 - 30.481}{0.8191}$$

$$= -12.6187 \quad \text{with } df = 249 + 79 - 2 = 326$$

Approximate p-value: Regardless of if we choose to use $df = 200$ or $df = 400$, a test statistic of $|-12.62| \Rightarrow$ a p-value < 0.0001 .

Conclusion: There is evidence of a difference in average fire efficiency between Western and Eastern dragons. Since $\bar{X}_W < \bar{X}_E$, there is evidence that Eastern dragons have higher average fire efficiency.

c) Outliers affect means and standard deviations which makes t-tests sensitive to outliers. If

the data is not normally distributed (has outliers) a Wilcoxon rank-sum test should be

considered. A log transformation could also be considered.